

Modeling Network Diversity for Evaluating the Robustness of Networks against Zero-Day Attacks

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Outline

- Introduction
- Modeling Network Diversity
 - Biodiversity-Inspired Metric
 - Least Attacking Effort-Based Metric
 - Probabilistic Metric
- Simulation
- Conclusion

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Why Worry about Zero-Day Attacks?

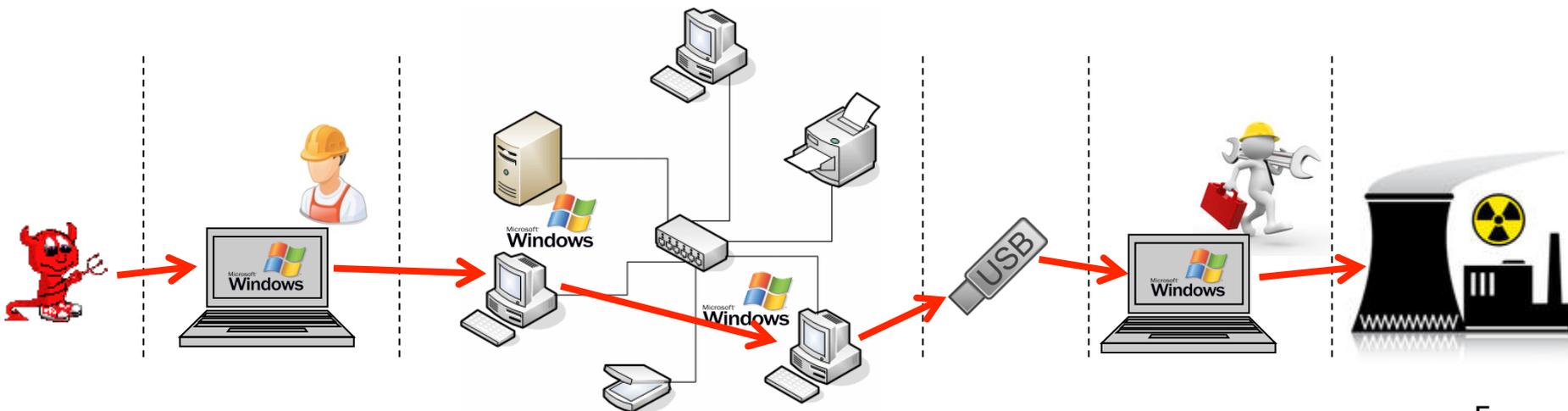
- ❑ A real threat to mission critical networks
- ❑ Governments and cybercriminals alike are stockpiling zero-day bugs¹
 - ❑ The NSA spent more than \$25 million a year to acquire software vulnerabilities - Edward Snowden
 - ❑ Private vendors provide at least 85 zero-day exploits on any given day of the year - Stefan Frei
 - ❑ E.g., Stuxnet exploits 4 different/complementary zero day vulnerabilities to infiltrate a SCADA network

- ❑ But what can we do about unknown attacks?

¹<http://krebsonsecurity.com/2013/12/how-many-zero-days-hit-you-today/>

How Could Diversity Help?

- ❑ Stuxnet's attack strategy
 - ❑ 3rd party (e.g., contractor) → organization's network → machine with Siemens Step 7 → PLC
- ❑ **The degree of software diversity along potential attack paths** can be considered a good metric for the network's capability of resisting Stuxnet



Existing Work on Diversity

- ❑ Software diversity has long been regarded as a security mechanism for improving robustness
- ❑ Tolerating attacks as Byzantine faults by comparing outputs or behaviors of diverse variants
- ❑ Opportunistic or automatically generated diversity (e.g., via randomization) improves the practicality
- ❑ Many new applications for diversity
 - ❑ Moving target defense (MTD)
 - ❑ Resisting worms in sensor networks
 - ❑ Improving robustness of network routing

So Why Another Paper?

- At a higher abstraction level, as a global property of an entire network, *network diversity* and its impact on security has not been formally modeled
 - How to define the diversity metric function? count?
how to count? ☾ * ◎ ■ ◆ ● ☾ ☽ ✕ ◆ ● ◇ □ × ○ □ ◇ ■ ■ ◆
 - How to apply the metric function? on the network as a multiset of resources? what about “paths”?
 - On which path? On one or more paths?
- It depends on the use cases...

Example Use Cases

- ❑ Worm propagation

 - ❑ Count *might* be sufficient

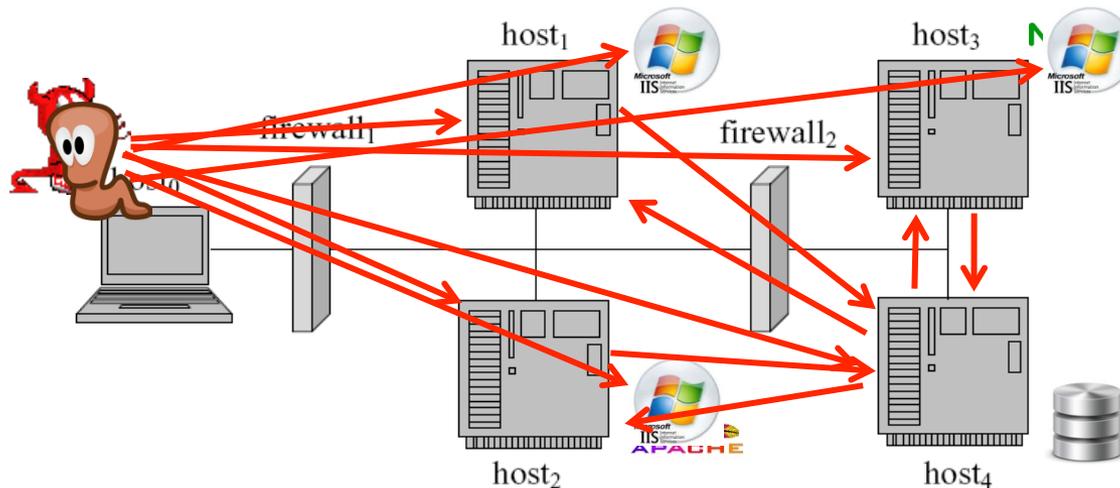
- ❑ Targeted attack (e.g.,

 - ❑ Least attack effort may

- ❑ MTD

 - ❑ The layers do not “combine” to increase attack effort

1. Intuitive notion of diversity can be misleading. A formal model is needed.
2. Different diversity metrics may be needed for different purposes.



Our Contribution

- We take the first step towards formally modeling network diversity as a security metric
 - We propose a network diversity function based on well known mathematical models of biodiversity in ecology
 - We design a network diversity metric based on the least attacking effort
 - We design a probabilistic network diversity metric to reflect the average attacking effort
 - We evaluate the metrics and algorithms through simulation
- The modeling effort helps understanding diversity and enables quantitative hardening approaches

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Bio-Diversity and Richness of Species

- A rich literature exists on biodiversity
 - Both theoretical studies and experiments confirm a positive relationship between biodiversity and the ecosystem's resistance to invasion and diseases
 - Many lessons may be borrowed, but we focus on metric functions and how they are applied
- *Richness* of species
 - The number of different species in an ecosystem
 - Problem: It ignores the relative abundance of each species



Effective Richness of Resources

□ *Effective number*¹

- *Shannon-Wiener index* (Shannon entropy using natural logarithm) groups systems with same levels of diversity
- The *effective number*, the exponential of this index, measures the number of equally-common species, even if in reality all species are not equally common.



- We define the *effective richness of resources* as:
(p_i is the relative frequency of resource i)

$$r(G) = \frac{1}{\prod_1^n p_i^{p_i}}$$

- Problem: Assuming all resources are equally different



Similarity-Sensitive Effective Richness

□ *Similarity-Sensitive Richness*¹

- Given a resource similarity function $z(\cdot): [1;m] \times [1;m] \rightarrow [0; 1]$ (with $z(i,i) = 1$), we define the effective richness of resources as:

$$r(G) = \frac{1}{\prod_1^n z p_i^{p_i}} \quad (z p_i = \sum_{j=1}^m z(i,j) p_j)$$

- We can simply talk about “the number of distinct resource types” from now on, as if all resources are equally common and equally different



¹T. Leinster and C.A. Cobbold. Measuring diversity: the importance of species similarity. *Ecology*, 93(3):477–489, 2012.

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From Food Web to Resource Graph

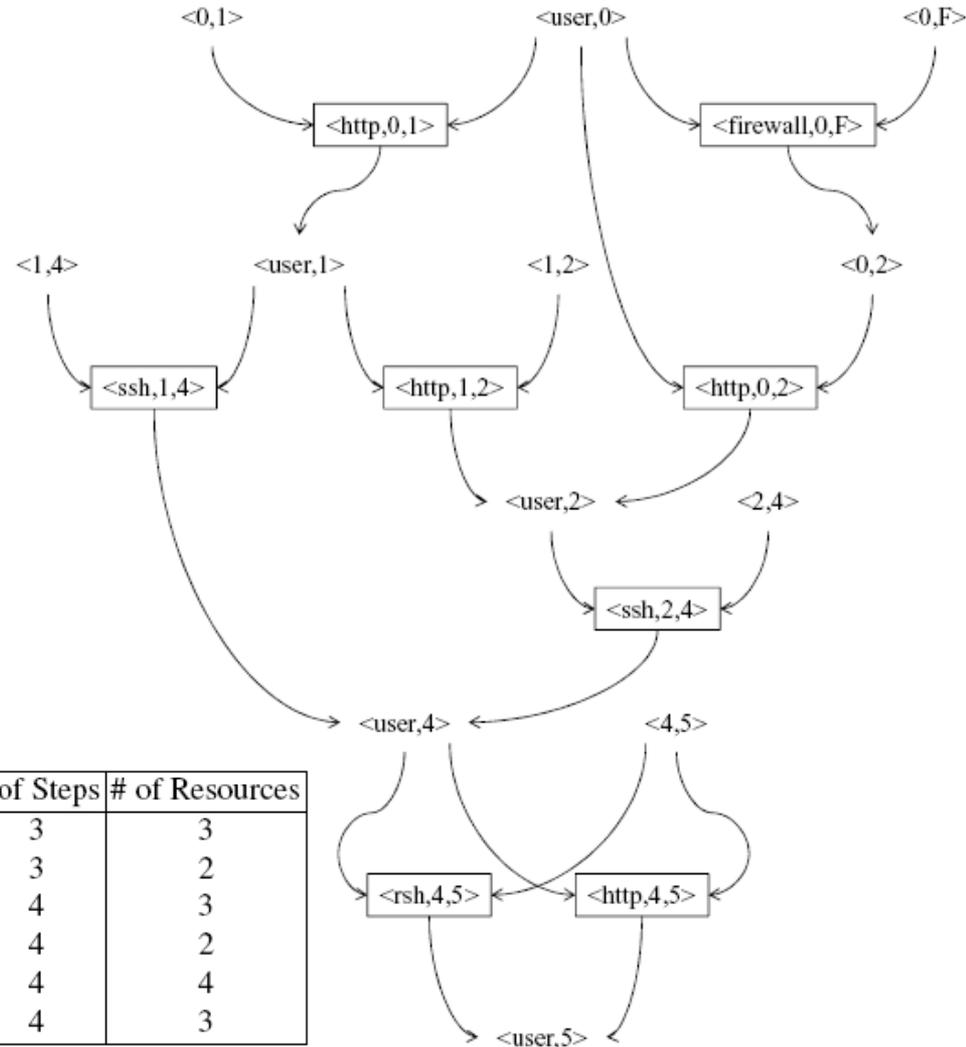
- The second lesson from biodiversity
 - The effect of biodiversity on stability of an ecosystem critically depends on the interaction of different species inside a food web¹
 - For food web, it is the feeding relationship (e.g., disease in one species affect those who feed on it)
 - For networks, it is the causal relationships (e.g., hacking one service may lead to accesses to others)
 - Resource graph
 - Syntactically equivalent to attack graph
 - Models causal relationships between network resources (instead of known vulnerabilities)

¹K.S. McCann. The diversity-stability debate. Nature, 405:228–233, 2000.

Resource Graph



- ❑ Vertices: zero day exploits of resources, their pre- and post-conditions
- ❑ Edges: AND between pre-conditions, OR between exploits
- ❑ On which path should we apply the diversity metric function (i.e., the number of distinct resource types)?



Attack Path	# of Steps	# of Resources
1. $\langle http, 0, 1 \rangle \rightarrow \langle ssh, 1, 4 \rangle \rightarrow \langle rsh, 4, 5 \rangle$	3	3
2. $\langle http, 0, 1 \rangle \rightarrow \langle ssh, 1, 4 \rangle \rightarrow \langle http, 4, 5 \rangle$	3	2
3. $\langle http, 0, 1 \rangle \rightarrow \langle http, 1, 2 \rangle \rightarrow \langle ssh, 2, 4 \rangle \rightarrow \langle rsh, 4, 5 \rangle$	4	3
4. $\langle http, 0, 1 \rangle \rightarrow \langle http, 1, 2 \rangle \rightarrow \langle ssh, 2, 4 \rangle \rightarrow \langle http, 4, 5 \rangle$	4	2
5. $\langle firewall, 0, F \rangle \rightarrow \langle http, 0, 2 \rangle \rightarrow \langle ssh, 2, 4 \rangle \rightarrow \langle rsh, 4, 5 \rangle$	4	4
6. $\langle firewall, 0, F \rangle \rightarrow \langle http, 0, 2 \rangle \rightarrow \langle ssh, 2, 4 \rangle \rightarrow \langle http, 4, 5 \rangle$	4	3

Selecting the Right Path(s)

- Intuitively, it should be the “shortest” path
 - 1 or 2, minimum # of steps? But 4 may take less effort than 1!
 - 2 or 4, minimum # of resources? But they both have 2 resources, so which one to choose, 2 or 4?
 - 4, minimizing (#steps/#of resources)? But what if there’s a path with 9 steps and 3 resources? $1/3 < 2/4$, but it clearly does not represent the least attack effort!

Attack Path	# of Steps	# of Resources
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Network Diversity in Least Attack Effort

- We define network diversity as:
 - (minimum # of resources on any path)/(minimum # of steps on any path)
 - Note: These may or may not be the same path! e.g., in this case: = 2 (path 2, 4) / 3 (path 1, 2)
 - The numerator 2 denotes the network's current level of diversity and the denominator 3 maximum potential (# of resources can never be greater than # of steps)

Attack Path	# of Steps	# of Resources
1. $\langle http, 0, 1 \rangle \rightarrow \langle ssh, 1, 4 \rangle \rightarrow \langle rsh, 4, 5 \rangle$	3	3
2. $\langle http, 0, 1 \rangle \rightarrow \langle ssh, 1, 4 \rangle \rightarrow \langle http, 4, 5 \rangle$	3	2
3. $\langle http, 0, 1 \rangle \rightarrow \langle http, 1, 2 \rangle \rightarrow \langle ssh, 2, 4 \rangle \rightarrow \langle rsh, 4, 5 \rangle$	4	3
4. $\langle http, 0, 1 \rangle \rightarrow \langle http, 1, 2 \rangle \rightarrow \langle ssh, 2, 4 \rangle \rightarrow \langle http, 4, 5 \rangle$	4	2
5. $\langle firewall, 0, F \rangle \rightarrow \langle http, 0, 2 \rangle \rightarrow \langle ssh, 2, 4 \rangle \rightarrow \langle rsh, 4, 5 \rangle$	4	4
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Complexity and Heuristic Algorithm

- Determining the network diversity is NP-hard
- Heuristic algorithm

- Only keep a limited number of local optima at each step

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Procedure Heuristic_Diversity
Input: Resource graph  $G(E \cup C, R_r \cup R_i)$ , goal condition  $c_g$ , parameter  $k$ 
Output:  $d_2$ 
Method:
1. For each  $e \in E$  and  $c \in C \setminus C_I$ 
2.   Mark  $e$  and  $c$  as unprocessed
3. For each  $c \in C_I$ 
4.   Mark  $c$  as processed
5.   Let  $\sigma(c) = \sigma'(c) = \phi$ 
6. While  $(\exists e \in E)(e \text{ is unprocessed})$  and  $(\forall c \in C)((c, e) \in R_r \Rightarrow c \text{ is processed})$ 
7.   Let  $\{c \in C : (c, e) \in R_r\} = \{c_1, c_2, \dots, c_n\}$ 
8.   Let  $\sigma(e) = \text{ShortestK}(\{q_1 \cup q_2 \cup \dots \cup q_n \cup \{e\} : q_i \in \sigma(c_i), 1 \leq i \leq n\}, k)$ 
9.   Let  $\sigma'(e) = \text{ShortestK}'(\{q_1 \cup q_2 \cup \dots \cup q_n \cup \{e\} : q_i \in \sigma(c_i), 1 \leq i \leq n\}, k)$ 
10.  Mark  $e$  as processed
11.  For each  $c$  s.t.  $(e, c) \in R_i$ 
12.    If  $(\forall e' \in E)((e', c) \in R_i \Rightarrow e' \text{ is processed})$  Then
13.      Let  $\sigma(c) = \text{ShortestK}(\bigcup_{e' \text{ s.t. } (e', c) \in R_i} \sigma(e'), k)$ 
14.      Let  $\sigma'(c) = \text{ShortestK}'(\bigcup_{e' \text{ s.t. } (e', c) \in R_i} \sigma(e'), k)$ 
15.    Mark  $c$  as processed
16. Return  $\frac{\min_{q \in \text{seq}(c_g)} |R(q)|}{\min_{q' \in \text{seq}(c_g)} |q'|}$ 
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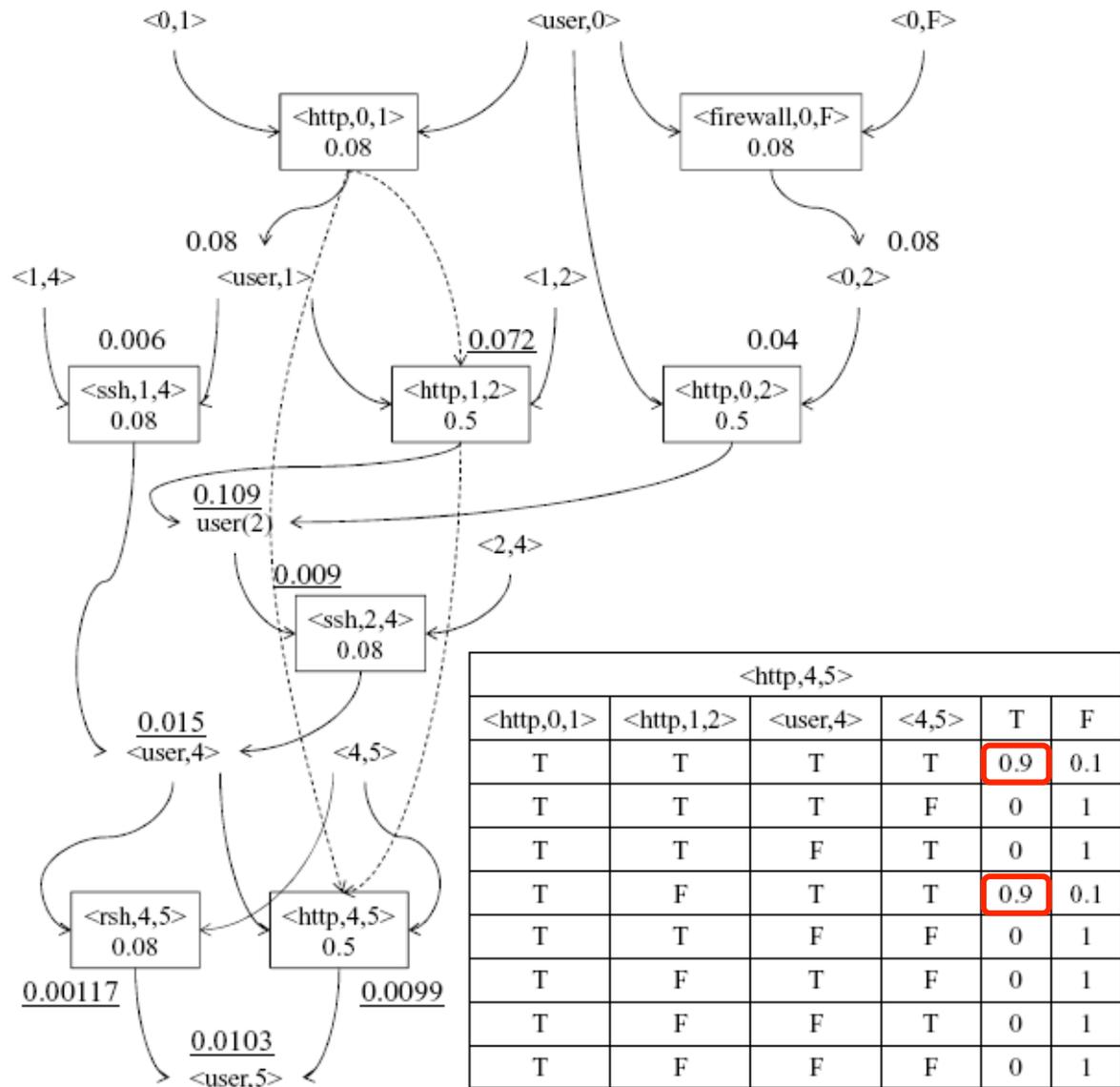
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Network Diversity in Average Effort

- The least attacking effort-based metric only provides a partial picture of the threat
- We now define a probabilistic network diversity metric based on the average attacking effort
- Informally, as p_1/p_2 , where
 - p_1 is the probability an attacker can compromise the given asset now, and
 - p_2 the probability he/she can still compromise it if all the resources were to be made different (i.e., every resource type would appear at most once)

An Example

- Number in smaller font: probability of an exploit given all pre-conditions are true
- Number in larger font: probability of reaching this node
- Dotted lines/
underlined numbers: given probabilities of reusing an exploit
- Network diversity = $0.007/0.0103$

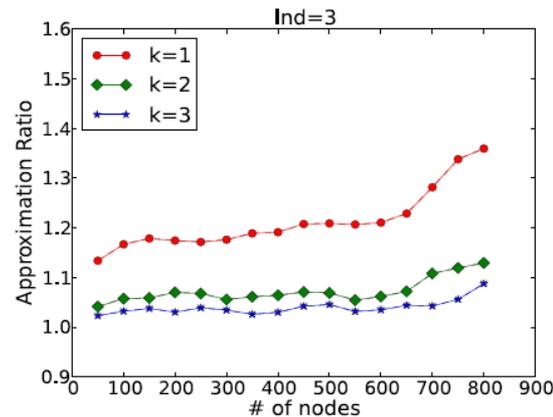
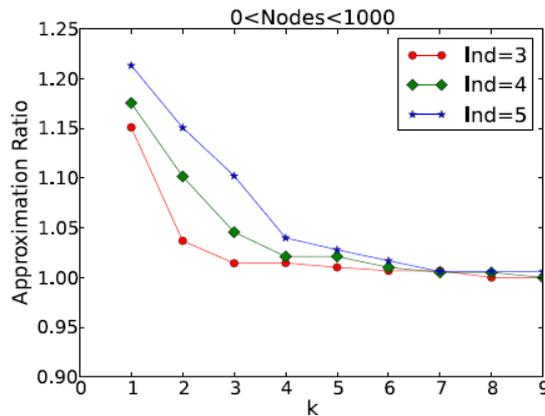


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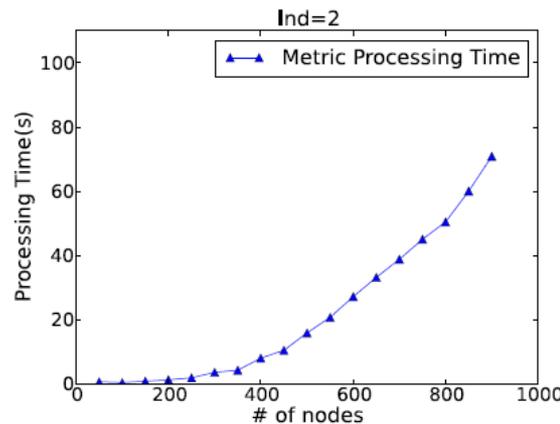
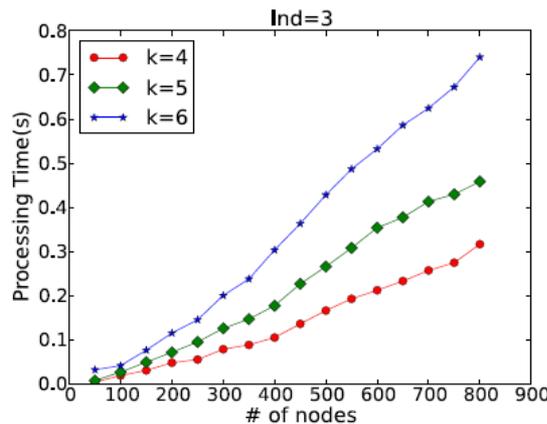
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Simulation Results

□ Accuracy/performance of the heuristic algorithm



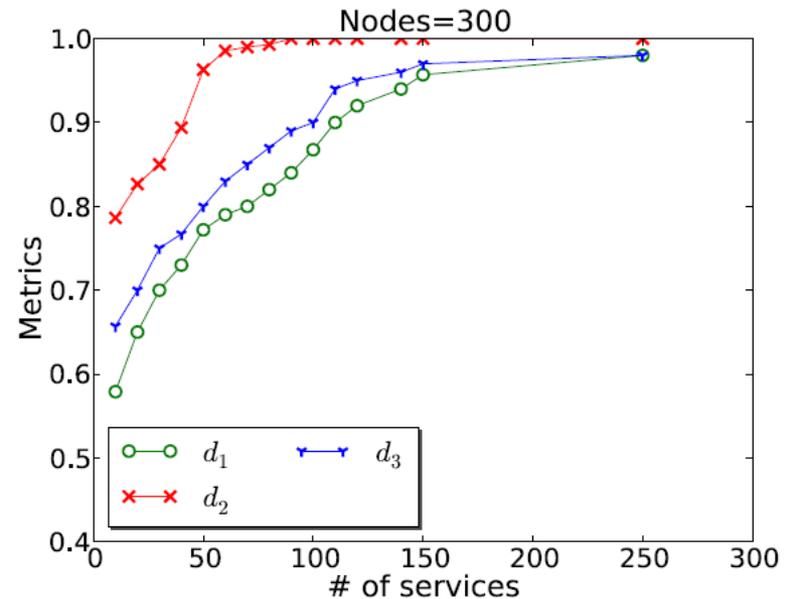
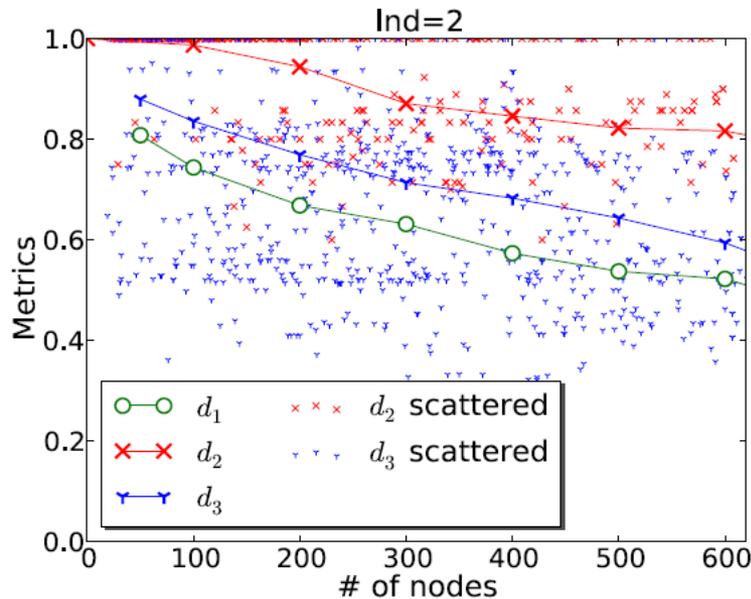
Approximation Ratio in k under Different In-degrees (Left) and in Graph Size under Different k (Right)



Processing Time for Computing d_2 in Graph Size under Different k (Left) and Processing Time for Computing d_3

Simulation Results Cont'd

□ Comparison of the metrics



Comparison of Metrics (Left) and the Effect of Increasing Diversity (Right)

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Conclusion

- ❑ We have taken a first step towards modeling network diversity, by proposing
 - ❑ a biodiversity-inspired metric
 - ❑ a least attacking effort-based metric
 - ❑ a probabilistic metric
- ❑ Limitations and future work
 - ❑ Depending on the availability and accuracy of inputs, e.g., resources, their relationships, and similarity
 - ❑ Simulations are based on random inputs
 - ❑ Not considering the cost and impact of diversity
 - ❑ Not considering the likelihood of attacks on resources
 - ❑ Future work will also apply other biodiversity results

Q & A

Thank You!

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